



Multiphase flow and reactive transport benchmark for radioactive waste disposal

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Abstract

Compacted bentonite is part of the multi-barrier system of radioactive waste repositories. The assessment of the long-term performance of the barrier requires using reactive transport models. Here we present a multiphase flow and reactive transport benchmark for radioactive waste disposal. The numerical model deals with a 1D column of unsaturated bentonite through which water, dry air and $\text{CO}_{2(g)}$ may flow and with the following reactions; aqueous complexation, calcite and gypsum dissolution/precipitation, cation exchange and gas dissolution. INVERSE-FADES-CORE V2, DuMu^X, TOUGHREACT and iCP were benchmarked with 6 test cases of increasing complexity, starting with conservative tracer transport under variably unsaturated conditions and ending with water flow, gas diffusion, minerals and cation exchange. The solutions of all codes exhibit similar trends. Small discrepancies are found in conservative tracer transport due to differences in hydrodynamic dispersion. Computed $\text{CO}_{2(g)}$ pressures agree when a sufficiently refined grid is used. Small discrepancies in $\text{CO}_{2(g)}$ and pH are found near the no-flow boundary at early times which vanish later. Discrepancies are due differences in the formulations used for gas flow at nearly water-saturated conditions. Computed $\text{CO}_{2(g)}$ pressures show a fluctuation between 10^{-4} and 10^{-3} years which slows down the in-diffusion of $\text{CO}_{2(g)}$. This fluctuation is associated with chemical reactions involving CO_2 . There are discrepancies in solute concentrations due to differences in the Debye–Hückel (DH) formulation. They are overcome when all codes use the same DH formulation. The results of this benchmark will contribute to increase the confidence on multiphase reactive transport models for radioactive waste disposal.

Keywords Benchmark · Reactive transport modelling · FEBEX bentonite · Multiphase flow

Introduction

Reactive Transport Modeling (RTM) is essential for comprehending the interconnected thermal, hydraulic, and chemical (THC) processes crucial for assessing the performance of geological disposal of radioactive waste, as highlighted in previous studies (Bildstein et al. 2019; Claret et al. 2018).

Benchmarks enhance the knowledge of novel challenges by apporportion the definition and the resolution of several test cases. Several code benchmark cases for reactive transport models have been proposed. The Groupe de Recherche Mathematical Modeling and Numerical Simulation for Nuclear Waste Management Problems (MoMaS) presented the benchmark of several cases representative of the problems encountered in nuclear waste disposal simulation (Carrayrou et al. 2010). According to De Dieuleveult and Erhel (2010), the main challenges of reactive transport simulations deal with solving strongly nonlinear systems with sharp

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fronts and stiff reactions. They reported oscillations due to numerical dispersion which were damped by refining the mesh. In Lagneau and van der Lee (2010), the authors also reported numerical oscillations for a system at thermodynamic equilibrium. Oscillations could be reduced by using a finer grid or by adding a kinetic control. In Alt-Epping et al. (2015), the authors presented a benchmark problem for reactive transport simulators based on a flow-through experiment carried out on saturated bentonite. The results for different codes showed excellent agreement. It was required to modify their thermodynamic databases (consistent activity coefficients and thermodynamic data) to achieve this good agreement. The FluidFlow study considers the injection of CO₂ into brine-saturated formations close to atmospheric conditions (Wapperom et al. 2024; Tian et al. 2024). They establish that the resolution and comparison of unstructured and Cartesian gridding reveals a high sensitivity of the overall distribution of CO₂ throughout the domain to gridding choices. They reported that the grid resolution plays a very important role in FluidFlow modeling. A refined grid is needed for a fully numerically converged solution. In Ahusborde et al. (2024) and De Hoop et al. (2024), the authors presented a benchmark case for CO₂ geological storage with focus on the coupling of two-phase flow and geochemistry. They showed that the results from all methods were comparable, even though there remained some discrepancies.

Previous subsurface environmental simulation benchmarks have stressed the need for benchmarking in the context of multiphase multicomponent reactive transport for radioactive waste disposal (Bildstein et al. 2021).

Here we report a multiphase flow and reactive transport benchmark for radioactive waste disposal. It is based on the conditions of the FEBEX (Full-scale Engineering Barrier Experiment) in situ test (Samper et al. 2018a, 2008; Zheng et al. 2011). The benchmark was performed with 4 multiphase flow and reactive transport codes (INVERSE-FADES-CORE V2, DuMu^X, TOUGHREACT and iCP) and involves 6 test cases of increasing complexity, including: conservative tracer migration, hydration under variably unsaturated conditions, gas diffusion, calcite and gypsum dissolution/precipitation, and cation exchange reactions.

In “Description of the benchmark: FEBEX in situ test” section, the paper starts with the description of the benchmark, including the mathematical formulation, the description of the FEBEX in situ test, the simplifications adopted for the benchmark and the main features of the model such as physical properties, space and time discretization, thermodynamic database, geochemical properties and initial and boundary conditions. Then, in “Description of the codes” section, the features of the computer codes utilized in the benchmark are presented. Afterwards, in “Comparison and discussion of the results” section, a selection of the benchmark results for test cases TC1 to TC6 are presented, followed by a comparative

analysis and discussion of results obtained by different teams. The paper ends with the main conclusions and perspectives for future work in “Conclusion and perspectives” section.

Description of the benchmark: FEBEX in situ test

In this section, a comprehensive description of the benchmark is presented. The multiphase mathematical formulation is outlined. Following this, the various proposed cases of increasing complexity are detailed to provide a clear understanding of the scenarios under consideration.

Multiphase mathematical formulation

This section presents the mathematical formulation of the coupled hydrological-chemical model. This formulation has been extracted from Zheng et al. (2011). Water mass balance is given by Navarro and Alonso (2000):

$$\frac{\partial (\Phi \rho_l X_l^w S_l + \Phi \rho_g X_g^v S_g)}{\partial t} + \nabla \cdot (\rho_l X_l^w \mathbf{q}_l + \rho_g X_g^v \mathbf{q}_g + \mathbf{j}_v) + r_w = 0, \quad (1)$$

where $\Phi (-)$ is the porosity, $S_\alpha (-)$ is the saturation degree of phase α ($\alpha \in \{l, g\}$). ρ_l and ρ_g (kg/m³) are the bulk densities of the liquid and gaseous phases, respectively, $X_l^w (-)$ is the mass fraction of water in the liquid phase, $X_g^v (-)$ is the mass fraction of the vapor in the gas phase, r^w (kg/m³/s) is the sink/source term of liquid water, \mathbf{q}_α (m/s) is the vector of volumetric flux of phase α which is given by Eq. 4, \mathbf{j}_v (kg/m²/s), is the dispersive mass flux of vapor with respect to the mean gas velocity which is given by Eq. 5. The dispersive mass fluxes of air and water with respect to the liquid phase are neglected.

The gas mass balance equation is given by:

$$\frac{\partial \Phi \rho_g S_g}{\partial t} + \nabla \cdot (\rho_g \mathbf{q}_g) + r_g = 0, \quad (2)$$

where r_g (kg/m³/s) is the sink/source term of gas. The dispersive mass flux of air and the gas with respect to the gaseous phase are neglected.

The air mass balance equation is given by:

$$\frac{\partial (\Phi \rho_g X_g^a S_g + \Phi \rho_l H S_l)}{\partial t} + \nabla \cdot (\rho_g X_g^a \mathbf{q}_g + \rho_l H \mathbf{q}_l) = 0, \quad (3)$$

where $X_g^a (-)$ is the mass fraction of air in the gaseous phase, $H (-)$ is the Henry's constant.

Our formulation assumes isothermal conditions and that all phases are at local thermal equilibrium and therefore they are all at the same temperature.

The volumetric flux \mathbf{q}_α (m/s) for each phase α ($\alpha \in \{l, g\}$), is given by:

$$\mathbf{q}_\alpha = -\frac{K_{ia}k_{ra}}{\mu_\alpha}(\nabla p_\alpha + \rho_\alpha g \nabla z), \quad (4)$$

where p_α (Pa) is the pressure of phase α , K_{ia} (m^2) is the intrinsic permeability tensor of the phase α , k_{ra} (–) is the relative permeability of the phase α , μ_α (Pa.s) is the viscosity of the phase α , z (m) is the elevation and g (m^2/s) is the gravitational acceleration.

The dispersive mass flux of vapor \mathbf{j}_v ($\text{kg}/\text{m}^2/\text{s}$) is calculated by the Fick's law:

$$\mathbf{j}_v = -\rho_g D_v \nabla X_g^v, \quad (5)$$

where D_v (m^2/s) is the hydrodynamic dispersion tensor for vapor which includes the effects of mechanical dispersion (D_{disp}) and molecular diffusion (D_v^e). The effective molecular diffusion coefficient for the vapor was calculated from Pollock (1986):

$$D_v^e = \frac{5.9 \cdot 10^{-6} \tau^v (T + 273.15)^{2.3}}{p_g}, \quad (6)$$

where τ^v (–) is the vapor tortuosity factor and T is the temperature expressed in Celsius.

It should be noticed that in the model the gases dissolved in water (air and other gases) are transported by advection and dispersion in the fluid phase together with liquid water.

Solute transport processes include advection, molecular diffusion, and mechanical dispersion. Each of them produces a solute flux per unit surface and unit time. There are as many transport equations as primary chemical species or aqueous components in the system. The primary species are the building blocks of chemical systems of interest, upon which concentrations of secondary species are written through laws of mass action for reactions at thermodynamic equilibrium.

The mass balance equation for the j -th primary species is given by Zheng and Samper (2008):

$$m_l^w \frac{\partial C_j}{\partial t} + \frac{\partial(m_l^w P_j)}{\partial t} + \frac{\partial(m_l^w W_j)}{\partial t} + \frac{\partial(m_l^w G_j)}{\partial t} = L^*(G_j) + r_j(C_j^0 - C_j), \quad (7)$$

where C_j (mol/L) is the total dissolved concentration of the of j -th primary species, m_l^w (kg/m^3) is the mass of liquid water per unit volume of medium, which is equal to $\rho^l X_l^w \theta_l$, where $\theta_l = S_l \Phi$ is the volumetric watercontent (m^3/m^3), P_j , W_j and G_j are the total precipitated minerals, the total exchanged and total dissolved gas concentrations (mol/L),

respectively, of the j -th primary species, r_j ($\text{kg}/\text{m}^3/\text{s}$) is the sink term, C_j^0 (mol/L) is the dissolved concentration of j -th species in the sink term r_j , N_c is the number of primary species. $L^*(\cdot)$ defines the transport operator as follows:

$$L^*(\cdot) = \nabla \cdot [m_l^w D^j \cdot \nabla(\cdot)] - m_l^w \mathbf{q}^l \cdot \nabla(\cdot) + (r_e - r_c)(\cdot), \quad (8)$$

where D^j (m^2/s) defines the dispersion coefficient including the hydrodynamic or mechanical dispersion and the porewater molecular diffusion while r_e and r_c are the condensation and evaporation rates ($\text{kg}/\text{m}^3/\text{s}$), respectively.

The reactive transport of the f -th gas species was implemented as an additional mass balance equation of the f -th gas species in the gaseous phase. The gas transport equation can be written in compact form as:

$$\rho_g \Phi S_g \frac{\partial C_f}{\partial t} = L_f^*(C_f) + r_f^i(C_f^o - C_f) + R_f, \quad (9)$$

where C_f (mol/kg) is the concentration of the of f -th gas species in the gaseous phase, r_f^i ($\text{kg}/\text{m}^3/\text{s}$) is the gas mass flux source entering, C_f^o (mol/kg) is the external concentration of the f -th gas species in the entering gas flux and R_f (mol/ m^3/s) is the gas chemical reactions term. Finally $L_f^*(\cdot)$ is the following transport operator:

$$L_f^*(\cdot) = \nabla \cdot [\rho_g \Phi S_g D^f \cdot \nabla(\cdot)] - \rho_g \mathbf{q}^g \cdot \nabla(\cdot), \quad (10)$$

where D^f (m^2/s) defines the dispersion coefficient including the mechanical dispersion and the molecular diffusion.

The chemical conceptual model for compacted bentonite accounts for the following reactions: aqueous complexation, acid/base, redox, cation exchange, mineral dissolution/precipitation (at equilibrium or in kinetic), and gas dissolution/exsolution. The chemical system is defined in terms of the concentrations of the primary species. The concentrations of the secondary species are computed from the concentrations of the primary species through appropriate mass action laws (Samper et al. 2009). The concentrations of the precipitated, exchanged and adsorbed species are computed using similar equations. A detailed description of the calculations of the chemical reactions can be found in Samper et al. (2009) and Zheng et al. (2011). The Gaines-Thomas convention is used for cation exchange. The total dissolved concentration C_j (mol/L), can be written in an explicit form as a function of the N_c primary species by applying the mass action law:

$$C_j = c_j + \sum_{k=1}^{N_x} \nu_{kj} x_k \quad (11)$$

$$= c_j + \sum_{k=1}^{N_x} \nu_{kj} \left(K_k^{-1} \gamma_k^{-1} \prod_{i=1}^{N_c} c_i^{\nu_{ki}} \gamma_i^{\nu_{ki}} \right)$$

where c_j (mol/L) is the dissolved concentration of the primary species j , N_x (–) is the number of secondary species, x_j (mol/L) is the concentration of the secondary species, K_k (–) is the equilibrium constant of the k -th secondary species reaction, γ (–) is the thermodynamic activity coefficient and ν_{kj} (–) is the stoichiometric coefficient of the j -th primary species on the k -th species.

The total concentration of the precipitated minerals of the j -th primary species, P_j (mol/L) can be written as:

$$P_j = \sum_{m=1}^{N_p} \nu_{mj}^p p_m, \quad (12)$$

where p_m (mol/L) is the concentration of the m -th mineral phase and ν_{mj}^p (–) is the stoichiometric coefficient of the j -th primary species on the m -th mineral.

Under equilibrium conditions, dissolution-precipitation reactions can be described by the mass action law which states that:

$$X_m \lambda_m K_m = \prod_{i=1}^{N_c} c_i^{\nu_{mi}} \gamma_i^{\nu_{mi}}, \quad (13)$$

where X_m (–) is the molar fraction of the m -th solid phase; λ_m (–) is the thermodynamic activity coefficient (X_m and λ_m are taken equal to 1 for pure phases); c_i (mol/L) and γ_i (–) are the concentration and activity coefficient of the i -th specie; ν_{mi} (–) is the stoichiometric coefficient in the dissolution reaction of the m -th solid phase; and K_m (–) is the corresponding equilibrium constant.

The concentration of the i -th exchanged cation (mol/L) can be obtained from the i -th equivalent fraction β_i , according to:

$$w_i = \beta_i CEC \rho_s \frac{(1 - \Phi)}{z_i 100 \Phi S_l} \quad (14)$$

$$= \left(K_{ij}^* \right)^{-\nu_i} c_i \gamma_i \left(\frac{\beta_j}{c_j \gamma_j} \right)^{\frac{\nu_i}{\nu_j}} CEC \rho_s \frac{(1 - \Phi)}{z_i 100 \Phi S_l},$$

where CEC (meq/100g) is the total cation exchange capacity, z_i (–) is the cation charge and K_{ij}^* (–) is the exchange coefficient or selectivity.

The total concentration of the dissolved gases concentrations of the j -th primary species G_j (mol/kg), can be written as:

$$G_j = \sum_{f=1}^{N_g} \nu_{jf}^g g_f, \quad (15)$$

where g_f (mol/kg) is the concentration of the f -th gas and ν_{jf}^g (–) is the stoichiometric coefficient of the j -th primary species on the f -th gas. For reactions involving aqueous and gas phases, the mass action law states that:

$$p_f \Gamma_f K_f = \prod_{i=1}^{N_c} c_i^{\nu_{fi}} \gamma_i^{\nu_{fi}}, \quad (16)$$

where p_f (Pa) is the partial pressure of the f -th species in the gas phase; Γ_f (–) is the activity coefficient and K_f (–) is the equilibrium constant of the reaction, c_i (mol/L) and γ_i (–) are the concentration and activity coefficient of the i -th dissolved primary species, ν_{fi} (–) is the stoichiometric coefficient of the f -th gas on the i -th specie. The gaseous phase is assumed as an ideal mixture and the fugacity constant, Γ_f is equal to 1.

The equilibrium constants for aqueous complexes and minerals depend on temperature. They are calculated with the following expression, which is valid for temperatures between 0 and 300 °C:

$$\log K(T) = \frac{b_1}{T^2} + \frac{b_2}{T} + b_3 \log T + b_4 + b_5 T, \quad (17)$$

where b_1 to b_5 are coefficients taken in the thermodynamic database of ThermoChimie v11.a (Giffaut et al. 2014), used for aqueous complexes and minerals.

For the activity coefficients of the aqueous species the extended Debye–Hückel formula can be used:

$$\log \gamma_i = \frac{-A z_i^2 (I)^{1/2}}{1 + B a_i (I)^{1/2}} + b I, \quad (18)$$

where I (–) is the ionic strength of the solution; z_i (–) and a_i (–) are the electric charge and the ionic radius in solution of the i -th species, respectively, A and B are constants which depends on the temperature and dielectric constant of water, and b is a constant determined from experimental data (A , B and b were taken from tabulated values from Helgeson and Kirkham (1974)). The value of the ionic strength is calculated as:

$$I = \frac{1}{2} \sum_{i=1}^{N_T} c_i z_i^2, \quad (19)$$

where N_T is the number of ions present in the solution.

The activity of the water can be calculated according to the approximation of Garrels and Christ (1965):

$$a_{H_2O} = 1 - 0.018 \sum_{i=2}^{N_T} c_i. \quad (20)$$

Description of the FEBEX in situ test reference case

The FEBEX in situ test was performed in a gallery excavated in granite in the underground research laboratory of Grimsel operated by NAGRA in Switzerland. The test included the heating system, the clay barrier and the instrumentation, monitoring and control system (Fig. 1).

The drift was 70.4 m long and 2.27 m in diameter. The test zone was located in the last 17.4 m of the drift where heaters, bentonite and instrumentation were installed. The main elements of the heating system were two heaters, separated horizontally by 1 m, which simulated full-sized canisters. The heaters were placed inside a cylindrical steel liner having a diameter of 0.93 m, which had been installed concentrically with the drift. Each heater was made of carbon steel, measured 4.54 m in length and 0.90 m in diameter, had a wall thickness of 0.10 m and weighed 11 tons. The heaters were designed to maintain a maximum temperature of 100 °C at the liner/bentonite interface. The bentonite barrier was made of blocks of highly compacted bentonite. The test began in February 1997. The first operation period lasted from 1997 to 2002 when heater 1 was switched off and the surrounding area was dismantled. The second operation period started after the emplacement of a shotcrete plug and ended in June 2015 when the entire bentonite barrier was fully dismantled.

The bentonite barrier is hydrated from the external cylindrical surface and water flows towards the internal heater/bentonite interface. The bentonite barrier is initially unsaturated, and it progressively hydrates from the surrounding rock towards the canister. The water content of the bentonite increases near the hydration boundary. Bentonite hydration leads to bentonite swelling. Therefore, the porosity of the bentonite increases during bentonite hydration. Mechanical and swelling processes play an important role in the hydrodynamic and geochemical evolution of the engineered barrier system during its early heating and hydration stage, when bentonite buffer is subjected simultaneously to heating and hydration.

The temperature is fixed at 100 °C on the heater/bentonite interface. Water evaporates near the heater. Vapor diffuses away from the heater and condenses in cooler places. Vapor condensation retards the hydration of the bentonite buffer and affects the concentration of the dissolved species (Villar et al. 2012; Zheng et al. 2011).

The conditions of the FEBEX in situ test call for a coupled non-isothermal multiphase flow conceptual model with: 1) Advection of water in the liquid phase; 2) Advection and diffusion of vapor and other gases in the gaseous phase; 3) Advection and diffusion of air in the liquid and gaseous phases; 4) Convection of heat in the liquid and gaseous phase and; 5) Heat conduction.

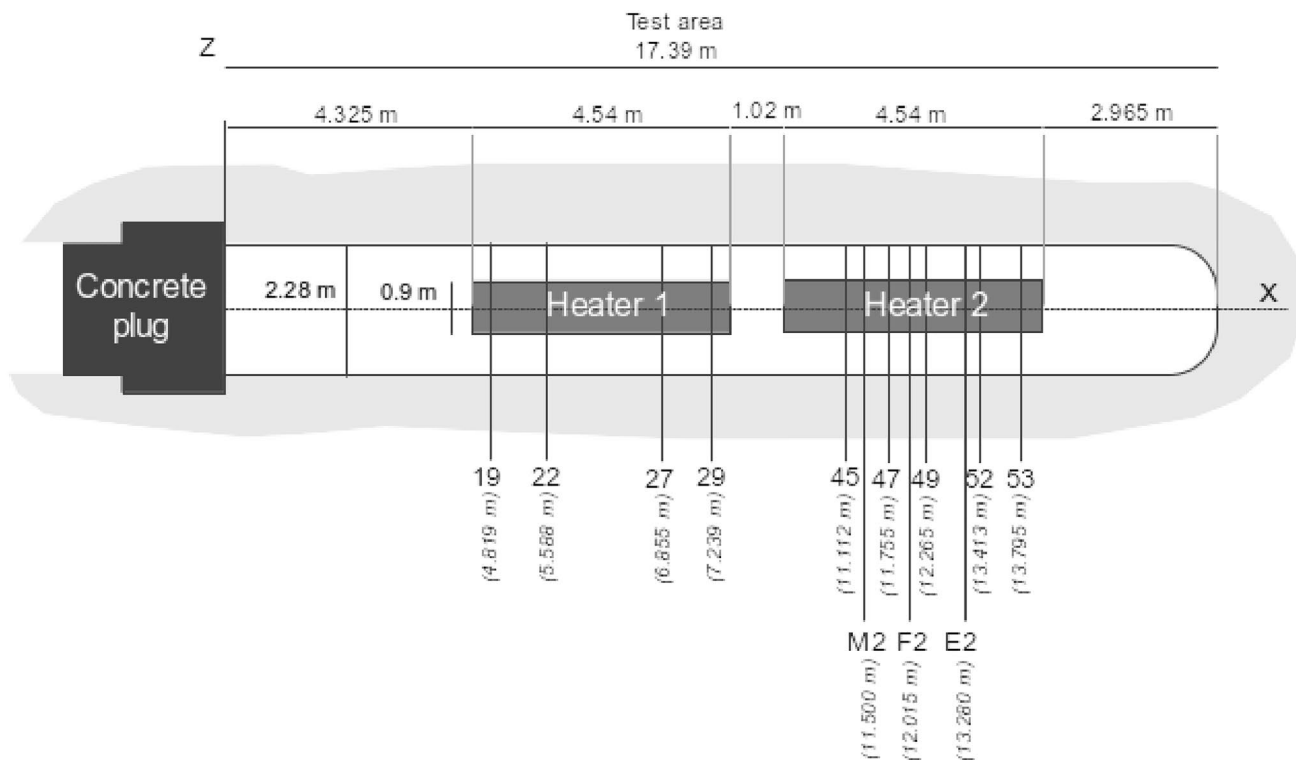


Fig. 1 General layout of the FEBEX in situ test indicating the instrumented and sampling sections used in this work. The x coordinates of the sections are referred to the concrete plug on the left

Simplifications and benchmark test cases

The conceptual model for the multiphase simulations needs to be simplified due to the complexity of the real system. It was agreed to consider a simplified system in the reference case and to increase the complexity of the modelled processes. The main simplification pertains to the temperature, which is assumed to be constant across all test cases, thus modeling isothermal processes. The proposed test cases (TC) are detailed in Table 1.

Model description

Physical properties

Table 2 shows the hydrodynamic and transport properties used in the numerical model of the FEBEX in situ test.

Time and space discretization

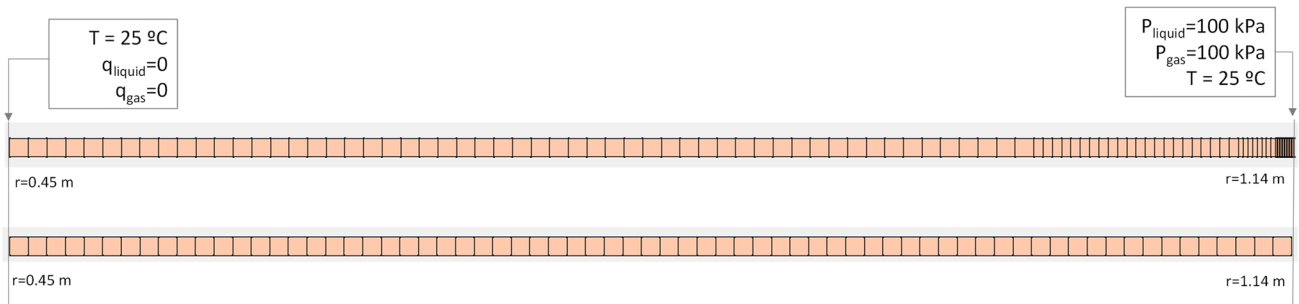
The numerical models were performed with two one-dimensional meshes. The first one is uniform (see bottom of Fig. 2). The grid size of the elements, denoted as Δx , is equal to 0.01 m throughout the entire domain. The second mesh,

Table 1 Description of benchmark test cases TC1 to TC6 for the FEBEX in situ test

	TC1	TC2	TC2B	TC3	TC3B	TC4	TC5	TC6
Hydration	Yes	No	No	No	No	Yes	Yes	Yes
Aqueous Species	Tracer	H ⁺ CO _{2(aq)} CO ₃ ²⁻	H ⁺ CO _{2(aq)} CO ₃ ²⁻ Ca ²⁺ Na ⁺ HCO ₃ ⁻ Cl ⁻ O _{2(aq)} OH ⁻ CaCl ⁺ CaCO ₃ Ca(OH) ⁺ NaCl CaCl ₂ Ca(HCO ₃) ⁺ Na(HCO ₃) Na(OH) Na(CO ₃) ⁻	H ⁺ CO _{2(aq)} CO ₃ ²⁻ Ca ²⁺	H ⁺ CO _{2(aq)} CO ₃ ²⁻ Ca ²⁺ Na ⁺ HCO ₃ ⁻ Cl ⁻ O _{2(aq)} OH ⁻ CaCl ⁺ CaCO ₃ Ca(OH) ⁺ NaCl CaCl ₂ Ca(HCO ₃) ⁺ Na(HCO ₃) Na(OH) Na(CO ₃) ⁻ H _{2(aq)}	H ⁺ CO _{2(aq)} CO ₃ ²⁻ Ca ²⁺	H ⁺ CO _{2(aq)} CO ₃ ²⁻ Ca ²⁺ Na ⁺ SO ₄ ²⁻	H ⁺ CO _{2(aq)} CO ₃ ²⁻ Ca ²⁺ Na ⁺ SO ₄ ²⁻ Cl ⁻ K ⁺ Mg ²⁺
Minerals	No	No	No	Calcite	Calcite	Calcite	Calcite Gypsum	Calcite Gypsum
Gases	Air	Air, CO _{2(g)}	Air, CO _{2(g)}	Air, CO _{2(g)}	Air, CO _{2(g)}	Air, CO _{2(g)}	Air, CO _{2(g)}	Air, CO _{2(g)}
Cation exchange	No	No	No	No	No	No	No	Na ⁺ , K ⁺ Ca ²⁺ , Mg ²⁺
Boundary $r = 1.14$ m	$P_g = 10^5$ Pa $P_l = 10^5$ Pa	$P_g = 10^5$ Pa $S_l = 60\%$ $X_g^{\text{CO}_2} = 0.1$	$P_g = 10^5$ Pa $S_l = 60\%$ $X_g^{\text{CO}_2} = 0.1$	$P_g = 10^5$ Pa $S_l = 60\%$ $X_g^{\text{CO}_2} = 0.1$	$P_g = 10^5$ Pa $S_l = 60\%$ $X_g^{\text{CO}_2} = 0.1$	$P_g = 10^5$ Pa $P_l = 10^5$ Pa $X_g^{\text{CO}_2} = 0.1$	$P_g = 10^5$ Pa $P_l = 10^5$ Pa $X_g^{\text{CO}_2} = 0.1$	$P_g = 10^5$ Pa $P_l = 10^5$ Pa $X_g^{\text{CO}_2} = 0.1$
	Prescribed granite boundary water		Prescribed granite boundary water	Prescribed granite boundary water	Prescribed granite boundary water	Prescribed granite boundary water	Prescribed granite boundary water	Prescribed granite boundary water

Table 2 Hydrodynamic and transport parameters (ENRESA 2006; Mon 2017; Samper et al. 2018a; Zheng and Samper 2008; Zheng et al. 2011, 2010)

Parameter	Value
Porosity, Φ (-)	$\Phi = 0.4$
Intrinsic permeability for liquid flow, K_{il} (m ²)	$K_{il} = k_o \frac{\Phi^3}{(1-\Phi)^2} \frac{(1-\Phi_o)^2}{\Phi_o^3}$ $k_o = 3.75 \times 10^{-21} \text{ m}^2$
Intrinsic permeability for gas flow K_{ig} (m ²)	$K_{ig} = 5 \times 10^{-10}$
Relative permeability to liquid, k_{rl} (-)	$k_{rl} = S_l^3$
Relative permeability to gas, k_{rg} (-)	$k_{rg} = (1 - S_l)^3$
Van Genuchten retention curve, Ψ (kPa)	$S_l = S_r + \frac{S_s - S_r}{\left(1 + \alpha \Psi^{\frac{1}{1-b}}\right)^b}$ $S_r = 0.05, S_s = 0.95$ $\alpha = 5 \times 10^{-5} \text{ kPa}^{-1}, b = 0.21$
Liquid viscosity μ_l (kg/(m.s))(T in Celsius)	$\mu_l = 661.2 \times 10^{-3} (T + 44)^{-1.562}$
Gas viscosity μ_g (kg/(m.s))	$\mu_g = 1.76 \times 10^{-5}$
Vapor tortuosity factor τ^v (-)	$\tau^v = 0.10$
Liquid density ρ_l (kg/m ³) (T in Celsius)	$\rho_l = 998.2 e^{(5 \times 10^{-7} (P_l - 100) - 2.1 \times 10^{-4} (T - 12))}$
Gas density ρ_g (kg/m ³) (T in Celsius)	$\rho_g = \rho_v + \rho_a$ $\rho_v = \frac{e^{(0.063747 - 0.1634 \times 10^{-3} T^2)}}{194.4} e^{-(2.16677 \Psi) / (\rho_l (T + 273.15))}$ $\rho_a = \frac{3.499 P_g}{T + 273.15} - 1.615 \rho_v$
Molecular diffusion in water D_o (m ² /s) at 25 °C	$D_o = 2 \times 10^{-11}$
Air Henry's constant H (-) (T in Celsius)	$H = \rho_l (T + 273.15) 7.1281183 \times 10^{-11} e^{\frac{1997.32}{T + 273.15}}$

**Fig. 2** Schematic of the meshes

composed of 104 nodes is represented in the upper part of the Fig. 2 and it is non uniform. Δx is equal to 0.01 m in the interval $0.45 \text{ m} < x < 1 \text{ m}$, Δx is equal to $5 \times 10^{-3} \text{ m}$ in the interval $1 \text{ m} < x < 1.1 \text{ m}$; Δx is equal to 2.5×10^{-3} in the interval $1.1 \text{ m} < x < 1.13 \text{ m}$; and Δx is equal to $6.25 \times 10^{-4} \text{ m}$ at the right boundary ($1.13 \text{ m} < x < 1.14 \text{ m}$). The model domain included the bentonite barrier, which extended from $r = 0.45 \text{ m}$ to $r = 1.14 \text{ m}$. The simulation time horizon covered the entire duration of the in situ test from February 1997 to 2015 (18 years).

Thermodynamic database

The benchmark cases consider the thermodynamic database ThermoChimie version 11a (Giffaut et al. 2014), available in different formats at <https://www.thermochimie-tdb.com/>.

Geochemical properties

The primary species considered in the geochemical model of the benchmark cases are the following: H_2O , H^+ , Na^+ , K^+ , Ca^{2+} , Mg^{2+} , Cl^- , SO_4^{2-} and CO_3^{2-} . Each test case includes different dissolves species and minerals which are shown in Table 1. Table 3 shows the chemical

Table 3 Chemical reactions and equilibrium constants for aqueous complexes, minerals, gases and selectivity constants for cation exchange reactions at 25 °C taken from the thermodynamic database ThermoChimie v11.a (Giffaut et al. 2014) to use in the model of the FEBEX in situ test benchmark case

Aqueous complexes	Log K
$\text{HCO}_3^- \rightleftharpoons \text{H}^+ + \text{CO}_3^{2-}$	– 10.3300
$\text{CO}_2(\text{aq}) + \text{H}_2\text{O} \rightleftharpoons 2\text{H}^+ + \text{CO}_3^{2-}$	– 16.6800
$\text{OH}^- + \text{H}^+ \rightleftharpoons \text{H}_2\text{O}$	14.000
$\text{H}_2(\text{aq}) + 0.5 \text{O}_2(\text{aq}) \rightleftharpoons \text{H}_2\text{O}$	+ 46.07
$\text{CaCl}^+ \rightleftharpoons \text{Ca}^{2+} + \text{Cl}^-$	+ 0.2900
$\text{CaCO}_3(\text{aq}) \rightleftharpoons \text{Ca}^{2+} + \text{CO}_3^{2-}$	– 3.2200
$\text{Ca}(\text{OH})^+ + \text{H}^+ \rightleftharpoons \text{Ca}^{2+} + \text{H}_2\text{O}$	+ 12.78
$\text{NaCl}(\text{aq}) \rightleftharpoons \text{Na}^+ + \text{Cl}^-$	+ 0.5000
$\text{CaCl}_2(\text{aq}) \rightleftharpoons \text{Ca}^{2+} + 2\text{Cl}^-$	+ 0.6400
$\text{Ca}(\text{HCO}_3)^+ \rightleftharpoons \text{Ca}^{2+} + \text{H}^+ + \text{CO}_3^{2-}$	– 11.43
$\text{NaHCO}_3(\text{aq}) \rightleftharpoons \text{Na}^+ + \text{H}^+ + \text{CO}_3^{2-}$	– 10.0800
$\text{Na}(\text{CO}_3)^- \rightleftharpoons \text{Na}^+ + \text{CO}_3^{2-}$	– 1.2700
$\text{Na}(\text{OH}) + \text{H}^+ \rightleftharpoons \text{Na}^+ + \text{H}_2\text{O}$	+ 14.75
Minerals	Log K
$\text{Calcite} \rightleftharpoons \text{Ca}^{2+} + \text{CO}_3^{2-}$	– 8.4800
$\text{Gypsum} \rightleftharpoons \text{Ca}^{2+} + \text{SO}_4^{2-} + 2\text{H}_2\text{O}$	– 4.6100
Gases	Log K
$\text{CO}_2(\text{g}) + \text{H}_2\text{O} \rightleftharpoons 2\text{H}^+ + \text{CO}_3^{2-}$	– 18.1500
Cation exchange	$K_{\text{Na-cation}}$
$\text{Na}^+ + \text{X-K} \rightleftharpoons \text{K}^+ + \text{X-Na}$	0.138
$\text{Na}^+ + 0.5 \text{X}_2 - \text{Ca} \rightleftharpoons 0.5 \text{Ca}^{2+} + \text{X-Na}$	0.294
$\text{Na}^+ + 0.5 \text{X}_2 - \text{Mg} \rightleftharpoons 0.5 \text{Mg}^{2+} + \text{X-Na}$	0.288

reactions and the equilibrium constants at 25 °C for the secondary aqueous species, minerals and gases used in the numerical model of the FEBEX in situ test benchmark case. Table 3 also depicts the selectivity constants for the cation exchange reactions in the bentonite. The total cation exchange capacity, CEC, is equal to 102.75 meq/100g.

Initial and boundary conditions

Bentonite had an initial porosity of 0.40, a volumetric water content of 24%, which corresponds to a gravimetric water content of around 14.4%, a liquid saturation degree of 60% and a suction of $1.17 \cdot 10^5$ kPa. The gas pressure was set to 100 kPa. The initial temperature was uniform, set at 25 °C, and assumed to remain constant. The initial compositions of the bentonite and the granite pore water, the initial mineral volume fractions

and the initial concentrations of exchanged ions are listed in Tables 4, 5 and 6 which can be found in the “Appendix”.

The temperature and the liquid and gas pressure at the outer boundary ($r = 1.14$ m) were equal to 25 °C and 100 kPa, respectively (see Fig. 2 and Table 1).

Description of the codes

Five teams participated in the benchmark with various codes. We are listing the different teams along with their codes, whose main features are described below.

- University of A Coruña (UDC) with INVERSE-FADES-CORE V2;
- University of Pau and the Adour Region (UPPA), with DuMu^X;
- Jilin University (JU) with TOUGHREACT;
- Technical University of Liberec (TUL) with iCP;
- Lithuanian Energy Institute (LEI) with iCP.

INVERSE-FADES-CORE V2: UDC

INVERSE-FADES-CORE V2 is a finite element code for modelling non-isothermal multiphase flow, heat transport and multicomponent reactive solute transport under both chemical equilibrium and kinetics conditions (Zheng and Samper 2015; Zheng et al. 2010). The code takes into account the mass balance of water, air, solid and enthalpy; the transport of solids and mechanical equilibrium. The solute transport equation accounts for advection, molecular diffusion, and mechanical dispersion. The reactive gas transport includes additional mass balance equations for the reactive gaseous species in the gaseous phase. The state variables for nonisothermal flow include liquid and gas pressures and temperature. INVERSE-FADES-CORE V2 solves both forward and inverse multiphase flow and multicomponent reactive transport problems in 1-, 2- and 3-D axisymmetric porous and fractured media. The code is the result of integrating the capabilities of a thermo-hydro-mechanical code FADES (Navarro and Alonso 2000), the reactive transport code CORE^{2D} (Xu et al. 1999), and the inverse methodology of INVERSE-CORE (Dai and Samper 2004). The code accounts for aqueous complexation, acid–base, redox, mineral dissolution/precipitation, gas dissolution/exsolution, cation exchange, and surface complexation reactions. INVERSE-FADES-CORE V2 solves first the multiphase flow and energy transport equations and then it solves for coupled transport processes and geochemical reactions by adopting the sequential iteration approach. Transport and chemical equilibrium equations are solved separately in an iterative sequential manner. At any given iteration, the chemical

sink/source term is assumed known (or taken equal to the value at the previous iteration) for the purpose of solving the transport equations. This renders the differential equations linear which allows the use of fast numerical methods for solving the linear system of equations. After solving the transport equations, the set of chemical equations is solved nodewise. The nonlinear chemical equations are solved with an iterative Newton–Raphson method. After convergence, the chemical source term is updated. The whole iterative process (transport and chemistry) is repeated until overall convergence is attained. The finite element method is used for spatial discretization, while implicit, explicit and Crank–Nicholson schemes are used for time discretization. INVERSE-FADES-CORE V2 has been used to model laboratory tests and in situ tests (Mon et al. 2023; Samper et al. 2018a, b, 2020a, b, 2008; Zheng and Samper 2008; Zheng et al. 2011, 2010, 2008).

DuMu^X: UPPA

DuMu^X (DUNE for Multi-Phase, Component, Scale, Physics,... flow and transport in porous media) (Koch et al. 2021) is a free and open-source simulator designed for modeling flow and transport processes in porous media. It is built on the Distributed and Unified Numerics Environment (DUNE) (Bastian et al. 2021), which is an object-oriented software framework written in C++. DUNE handles essential computational tasks such as input/output operations, memory management, grid generation, and parallel computing.

Over the years, UPPA has contributed to DuMu^X by implementing various numerical schemes for reactive transport modeling. In particular, works such as Ahusborde et al. (2015, 2018) and Ahusborde and El Ossmani (2017) introduced a sequential approach that decomposes the global problem into two sub-problems. The first sub-problem addresses two-phase compositional flow, where only species present in both phases are treated implicitly, and phase exchanges are fully resolved in this step, while other species are treated explicitly. The second sub-problem involves solving a reactive transport problem, using the flow properties (e.g., Darcy velocity, phase saturations, temperature, and phase densities) computed in the first step. In Ahusborde et al. (2015) and Ahusborde and El Ossmani (2017), a sequential iterative approach (SIA) was utilized for the reactive transport sub-problem. However, to mitigate potential time-splitting errors associated with SIA, a global implicit approach was adopted in Ahusborde et al. (2018). Subsequent developments led to the creation of a fully implicit, fully coupled method using a direct substitution approach, as detailed in Ahusborde et al. (2019, 2021). More recently, these methodologies have been extended to study coupled Thermo-Hydro-Chemical processes for both fully

implicit and sequential approaches (Ahusborde et al. 2023). This contribution focuses solely on results derived from the fully implicit approach.

The spatial discretization employs a cell-centered finite volume (FV) scheme. Convective terms are approximated using a fully upwind scheme, while diffusive terms are calculated using a two-point flux approximation (TPFA). This approach is suitable for the orthogonal meshes used in the benchmark geometries. For more complex meshes, multi-point flux approximations (MPFA) could be implemented. The nonlinear system is resolved using a Newton–Raphson algorithm, with the Jacobian matrix approximated by numerical differentiation. The resulting linear systems are solved using the BiConjugate Gradient STABILIZED (BiCGSTAB) method, preconditioned with an Algebraic Multigrid (AMG) solver. An adaptive time-stepping strategy, based on the iteration count of the Newton method from the previous time step, is employed. A comprehensive description of our methodology is provided in Ahusborde et al. (2021, 2023). This methodology has been validated through multiple test cases, including high-performance computing applications and studies on the geological storage of CO₂ in deep saline aquifers.

TOUGHREACT : JU

TOUGHREACT is a code for simulating non-isothermal multiphase fluid flow, heat transport and multicomponent reactive solute transport (Xu and Pruess 1998; Xu et al. 2006, 2011). It has been developed by introducing reactive transport into the existing framework of a non-isothermal multi-component fluid and heat flow simulator TOUGH2 (Pruess et al. 1999). A series of subsurface thermo-physical-geochemical processes are considered under various thermo-hydrological and chemical conditions of pressure, temperature, water saturation, and ionic strength. TOUGHREACT can be used in one-, two-, or three dimensional porous and fractured media with physical and chemical heterogeneity. The first version of the TOUGHREACT code was released to the public through the US Department of Energy's Energy Science and Technology Software Center (ESTSC) in August 2004. The mass and energy balance equations in TOUGHREACT are solved by Newton–Raphson iterations and proceeds as in TOUGH2 (Pruess et al. 1999). Space discretization involves an unstructured finite volume scheme (Integral Finite Differences, IFD). Given the chemical transport equations have the same structure as the fluid and heat flow equations, the transport equations can be solved by the same numerical method. TOUGHREACT uses a sequential iteration approach. After solution of the flow equations, the fluid velocities and phase saturations are used for chemical transport modeling. The chemical transport is solved

on a basis of component-by-component. The resulting concentrations obtained from solving transport equations are substituted into the chemical reaction model. The system of mixed equilibrium-kinetic chemical reaction equations is solved on a grid block by grid block basis by Newton-Raphson iteration. Optionally, the chemical transport and reactions are solved iteratively until convergence. The TOUGHREACT code has been widely applied for studies in CO₂ geological sequestration (Gherardi et al. 2007; Hu et al. 2023b, 2019; Zhu et al. 1999), geothermal resources development (Chen et al. 2020; Spycher et al. 2014; Wanner et al. 2014), nuclear waste isolation (Xu et al. 2008), and increasingly for petroleum applications (Hu et al. 2023a).

iCP: TUL and LEI

iCP v2.1 is an interface developed by Amphos21 (Spain) to couple two standalone simulation programs: the general-purpose finite element platform COMSOL Multiphysics (COMSOL 2022) and the geochemical code PHREEQC (Parkhurst and Appelo 2013). The main goal of the interface is to take advantages and capabilities of mentioned codes, providing a numerical platform that can efficiently simulate a wide number of multiphysics problems coupled with geochemistry. iCP is written in Java and uses the IPHREEQC++ dynamic library and the COMSOL Java-API (Nardi et al. 2014).

COMSOL Multiphysics (COMSOL 2022) is a commercial finite element code with a set of predefined physics interfaces widely used in various industrial applications. Alternatively, input of user's own partial differential equation is possible through the Partial Differential Equation (PDE) Interface. Then, COMSOL Multiphysics provides the coupling between the individual equations by either a fully coupled or segregated solver. The polynomial order of the finite element base (shape) functions can be chosen by the user. The default settings were used, linear for the transport equations and quadratic for the flow.

PHREEQC (Parkhurst and Appelo 2013) is a free general geochemical code developed by U.S. Geological Survey for simulating chemical reactions and transport processes in water. The program is based on equilibrium chemistry of aqueous solutions interacting with minerals, gases, solid solutions, exchangers, and sorption surfaces, which accounts for the original acronym: pH-REdox-Equilibrium (Parkhurst and Appelo 2013). Although a broader functionality is also included in PHREEQC, the equilibrium reactions were only used in this benchmark. The program uses a modified Newton-Raphson method to solve the simultaneous nonlinear equations (Parkhurst and Appelo 1999).

The coupling between the physical processes solved by COMSOL Multiphysics (water flow, water-phase species

transport, and gas-phase diffusion) and chemical reactions solved by PHREEQC is realised by the operator splitting method, also called Sequential Non Iterative Approach (SNIA) (Nardi et al. 2022). In a single time step controlled by the iCP user setting, the two models run one by one. COMSOL is based on the Finite Element Method and, therefore, the variables (i.e. concentrations) are calculated at the nodes of the mesh. These node concentrations are transferred to PHREEQC at every communication step to perform the chemical calculations. The model can be divided in chemical domains with different geochemical systems (i.e. with different mineralogy). Nodes at the interface of two or more chemical domains are calculated for each domain. The resulting concentrations are arithmetically averaged, assigned to the node and transferred to COMSOL (Nardi et al. 2022). The chemical step is parallelized by grouping sets of nodes and solving them on different PHREEQC instances. These PHREEQC instances are solved on different executable threads by means of the internal thread library of Java (shared memory approach) (Nardi et al. 2022).

iCP interface make additional physics interface available in COMSOL Multiphysics platform named “Molal solute transport by advection–diffusion”. This interface was used in transport simulations of a number of chemical species and could be coupled to other interfaces in COMSOL Multiphysics. For modelling of water mass balance in the porous media and CO₂ transport in predefined test cases the physics interfaces “Richard’s equation” and “Transport of Diluted Species in Porous Media” were used additionally respectively. Parameter input to the latter interfaces as well as the solver settings and timestepping for iCP requires definition by the user, therefore these inputs may not be unique among the iCP users. Running PHREEQC for the benchmark cases required a non-standard use of its input control. It is made to be run with the full set of species and reactions in the thermodynamic database. Therefore, a reduced database file was created, containing only the species and reactions in the respective Test Case and water. The activity coefficients were not input explicitly but evaluated by PHREEQC via the implemented Debye–Hückel model. The resulting values were checked against the prescribed ones. Contrary to most other reactive transport codes, PHREEQC requires enforcing charge balance at all times, including the initial conditions and in all boundary waters. To compare the results of INVERSE-FADES-CORE V2, TOUGHREACT and DuMu^X with those of iCP, charge balance was enforced by adding two dummy charged unreactive species. Cl[−] and Na⁺ were selected as the dummy unreactive species with appropriate concentrations to ensure charge balance. These species are included in the geochemical system, contribute to the

total ionic strength of the aqueous dissolved system and affect the chemical activities of the dissolved species.

Comparison and discussion of the results

In this section, we conduct a comparative analysis of results obtained from different numerical codes. To maintain conciseness, we present only a subset of the computed results from participants, with the full set available as supplementary data. In the figures, the teams are identified by the abbreviated name of the code used as follows: UDC is represented as F-CORE, UPPA as DuMu^X, JU as T-REACT, LEI as iCP-1, and TUL as iCP-2. All test cases were completed by each code, except for test cases TC2B and TC3B, which were only performed by F-CORE and iCP-1.

Case TC1. Hydration and conservative tracer.

Case TC1 deals with single-phase variably-saturated water flow and conservative solute transport. Bentonite hydration was simulated by prescribing the liquid pressure equal to 100 kPa at the right boundary ($r = 1.14$ m). A constant temperature of 25 °C was considered in this case. The total time of simulation was 18 years. The computed water content increases with time (Fig. 3a) due to the inflow of water from the right boundary ($r = 1.14$ m). The concentration of the tracer decreases near the right boundary because the concentration of the inflow water (1.3×10^{-5} mol/L) is smaller than the initial concentration (1.6×10^{-1} mol/L) (see Fig. 3b). The tracer concentration front displaces due to advection and spreads due to diffusion and dispersion.

Case TC1 was simulated by 5 teams. The water contents computed by different teams agree for the most part. However, there are small discrepancies of about 0.005 near the left boundary ($r = 0.45$ m) at $t = 18$ years (Fig. 3a). The spatial distribution of the computed tracer concentrations is similar for most teams. However, there are small differences at the tracer front. These differences are possibly related to differences in hydrodynamic dispersion because advection is the dominant transport mechanism. The concentrations computed by F-CORE and iCP-1 coincide in the case of no water flow (only solute diffusion) (see Fig. S1 in Supplementary Material). Model sensitivity runs show that the tracer concentrations are sensitive to changes in the longitudinal dispersivity, the diffusion coefficient, and the water flow (see Fig. S2 in Supplementary Material).

Case TC2 and TC2B. No hydration and gas diffusion

Case TC2 deals with $\text{CO}_{2(g)}$ gas diffusion and aqueous chemical reactions by considering H^+ , $\text{CO}_{2(aq)}$ and CO_3^{2-} as

secondary species in the reactive transport model. The partial pressure of $\text{CO}_{2(g)}$ was prescribed at 0.1 bar at the right boundary ($r = 1.14$ m). $\text{CO}_{2(g)}$ partial pressure in the bentonite increases with time (Fig. 3d). The partial pressure of $\text{CO}_{2(g)}$ becomes uniform after 2 days and equal to the prescribed pressure. Aqueous $\text{CO}_{2(aq)}$ is in equilibrium with gaseous $\text{CO}_{2(g)}$ and therefore, the increase in $\text{CO}_{2(g)}$ pressure leads to an increase in the concentration of dissolved $\text{CO}_{2(aq)}$ and a decrease in pH (Fig. 3c, e).

Case TC2 was simulated by 5 teams. The $\text{CO}_{2(g)}$ partial pressure computed by different teams agree for the most part. However, there are small discrepancies near the left boundary ($r = 0.45$ m) in the computed pH and $\text{CO}_{2(aq)}$ at early times ($t < 0.1$ days). These discrepancies are related to the limited accuracy of the numerical solution provided by the numerical grid. The largest discrepancy in $\text{CO}_{2(aq)}$ is approximately equal to 1.5×10^{-4} mol/L at $t = 0.1$ days.

Case TC2B is based on case TC2 and includes additional secondary species to ensure charge balance in the reactive transport model (see Table 1). The computed results for cases TC2B and TC2 are similar (Fig. 3f), except for the computed pH. The computed pH in case TC2B is smaller than that of case TC2. Case TC2B test case was simulated by 2 teams (Fig. 3f). Similar to case TC2, small discrepancies in pH are found in case TC2B near the left boundary at early times.

Computed $\text{CO}_{2(g)}$ partial pressure increases with time until $t = 0.01$ years when the pressure becomes equal to the prescribed pressure at the boundary (Fig. 4a). The computed pH shows a trend opposite to that of CO_2 because it decreases until $t = 0.01$ years to 7.72. The results computed for case TC2 by 5 teams involved agree for the most part (Fig. 4c).

Case TC3. No hydration, gas diffusion and mineral dissolution/precipitation

Case TC3 deals with gas diffusion and calcite dissolution/precipitation. Water saturation remains constant and equal to 60% while the $\text{CO}_{2(g)}$ partial pressure was prescribed equal to 0.1 bar at the right boundary ($r = 1.14$ m). Case TC3 takes into account calcite dissolution/precipitation. Concentrations of dissolved species decrease near the right boundary because the concentrations prescribed at the right boundary are smaller than the initial concentrations. Similar to case TC2, the partial pressure of $\text{CO}_{2(g)}$ becomes uniform and equal to the prescribed gas pressure at $t = 2$ days (Fig. 5a). The increase in the concentration of $\text{CO}_{2(aq)}$ leads to a decrease in pH (Fig. 5c). In addition, calcite precipitates in a thin band of a few mm near the right boundary (Fig. 5b).

Case TC3 was simulated by 5 teams. The $\text{CO}_{2(g)}$ partial pressure computed by different teams agree for

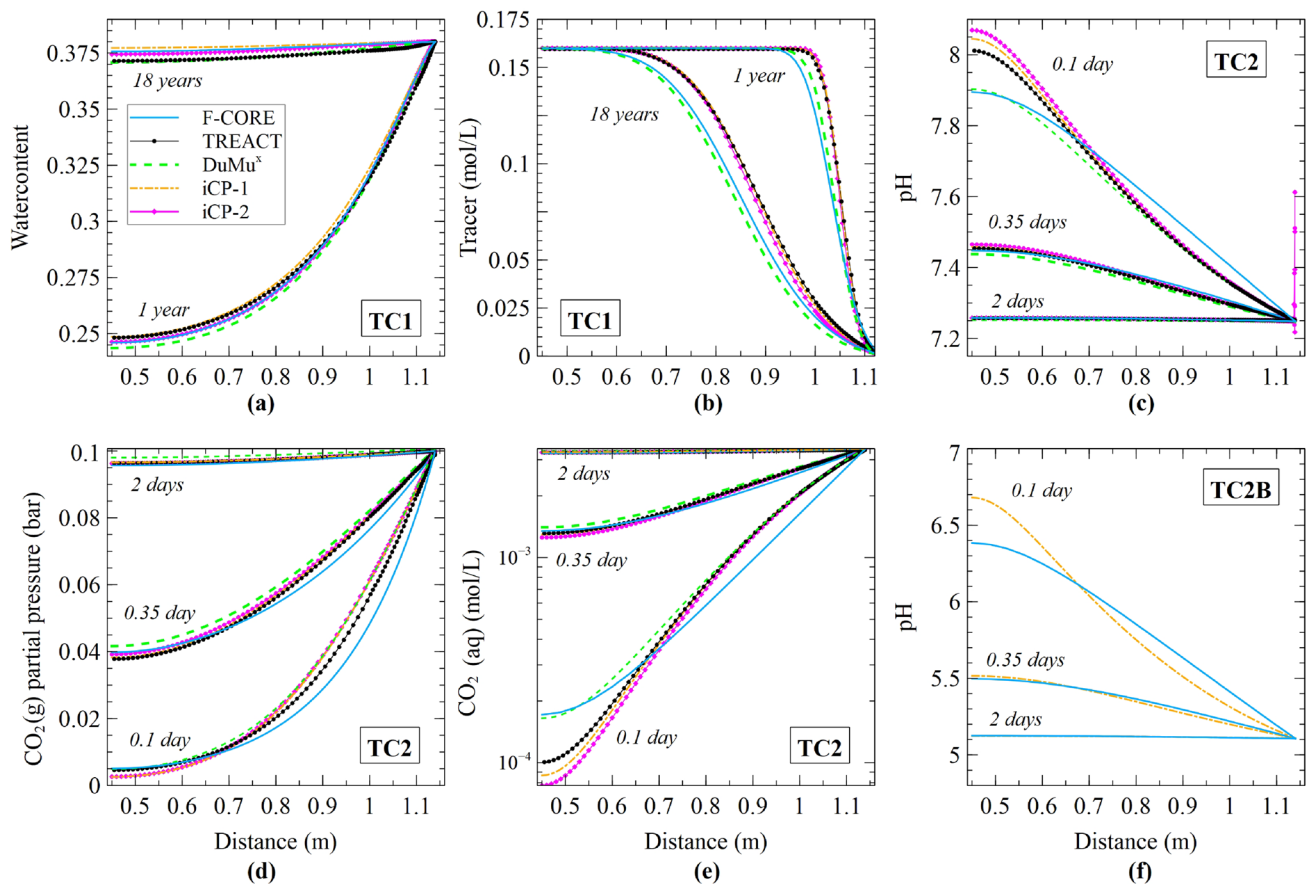


Fig. 3 Benchmarking of the spatial distribution of computed: **a** Water contents for case TC1 at $t = 1$ and $t = 18$ years; **b** Tracer concentrations for case TC1 at $t = 1$ and $t = 18$ years; **c** pH for cases TC2 at $t = 0.1$, $t = 0.35$ and $t = 2$ days; **d** Partial pressure of $\text{CO}_{2(g)}$ for case

TC2 at $t = 0.1$, $t = 0.35$ and $t = 2$ days; **e** Concentration of dissolved $\text{CO}_{2(aq)}$ for case TC2 at $t = 0.1$, $t = 0.35$ and $t = 2$ days; and **f** pH for cases TC2B at $t = 0.1$, $t = 0.35$ and $t = 2$ days

the most part (Fig. 5a). However, there are some small discrepancies near the left boundary which translate also into small discrepancies in the computed pH at early times. The spatial distribution of the computed calcium concentrations is similar for most teams (Fig. 5d). However, small differences are found at the concentration front similar to those of case TC1. Computed calcite precipitation and pH spatial distribution coincides for most teams.

Case TC3B is similar to case TC3 and incorporates additional secondary species (see Table 1). The computed results in case TC3B show calcite dissolution instead of calcite precipitation in case TC3. This test case was simulated by 2 teams. The computed $\text{CO}_{2(g)}$ partial pressure, dissolved $\text{CO}_{2(aq)}$ concentration, pH and dissolved Ca^{2+} concentrations results for cases TC3B and TC3 are similar (Fig. 5e, f). There are small discrepancies in the computed pH and calcite.

Case TC4. Hydration, gas diffusion and mineral dissolution/precipitation

Case TC4 deals with liquid flow and gas diffusion and considers the geochemical system of case TC3. The computed water content increases with time due to the water inflow which was described in case TC1 (Fig. 3a). The effective diffusion coefficient of the $\text{CO}_{2(g)}$ decreases at the right boundary due to the water inflow through the right boundary. The diffusion of $\text{CO}_{2(g)}$ is slower than in cases TC2 and TC3 due to the increase of water saturation. The time needed for the partial pressure of $\text{CO}_{2(g)}$ to become uniform in case TC4 is about 20 days (Fig. 6a). This time is much larger than the times required in cases TC2 and TC3. The computed concentration of dissolved Ca^{2+} decreases near the right boundary because the concentration of the boundary water is smaller than the initial concentration. In addition, calcite precipitates in the bentonite and especially in a thin band of a few mm near the right boundary at early times (Fig. 6b). Calcite precipitation consumes dissolved

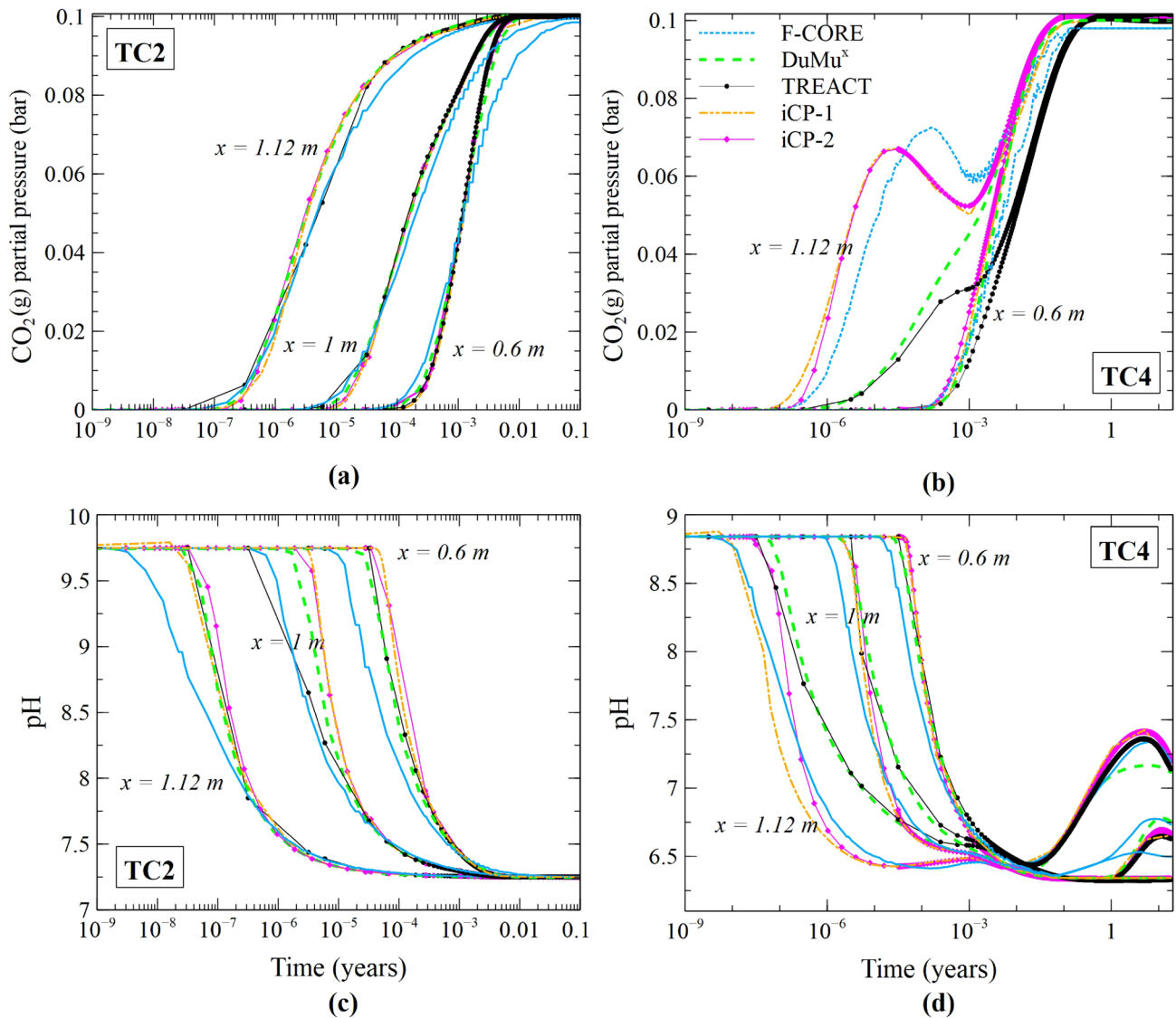


Fig. 4 Benchmarking of the time evolution of computed: **a** Partial pressure of $\text{CO}_{2(\text{g})}$ for case TC2 at $x = 1.12 \text{ m}$, 1 m and 0.6 m ; **b** Partial pressure of $\text{CO}_{2(\text{g})}$ for case TC4 at $x = 1.12 \text{ m}$ and 0.6 m ; **c** pH for

case TC2 at the distances $x = 1.12 \text{ m}$, 1 m and 0.6 m ; and **d** pH for case TC4 at the distances $x = 1.12 \text{ m}$, 1 m and 0.6 m

calcium (Fig. 6c). pH decreases in the bentonite while $\text{CO}_{2(\text{g})}$ diffuses into the bentonite. However, pH increases when calcite precipitates near the right boundary. The calcite precipitation front in case TC4 penetrates into the bentonite about 35 cm at the end of the simulation (18 years). The computed pH decreases in the bentonite as the dissolved $\text{CO}_{2(\text{g})}$ diffuses into the bentonite and increases near the right boundary due to calcite precipitation (Fig. 6d).

Case TC4 was simulated by 5 teams. The computed $\text{CO}_{2(\text{g})}$ partial pressures by different teams follow the same trends (Fig. 6a). However, there are some discrepancies in the diffusion profile. These discrepancies are caused by differences in the formulations implemented in different codes for gas flow at the transition from unsaturated to

nearly saturated conditions. The computed $\text{CO}_{2(\text{g})}$ partial pressures are very sensitive to mesh discretization. The gas diffusion profiles computed by different teams with a uniform mesh show significant differences (see Fig. S3 in Supplementary Material). These differences are less relevant when a more refined grid is used.

The concentrations of dissolved Ca^{2+} computed by different teams are similar. However, there are small differences at the concentration front similar to those reported for previous cases. Computed calcite precipitation and pH spatial distribution trends coincides for most teams.

The diffusion of $\text{CO}_{2(\text{g})}$ is fast. Steady and uniform pressures are reached in less than a year. Model results

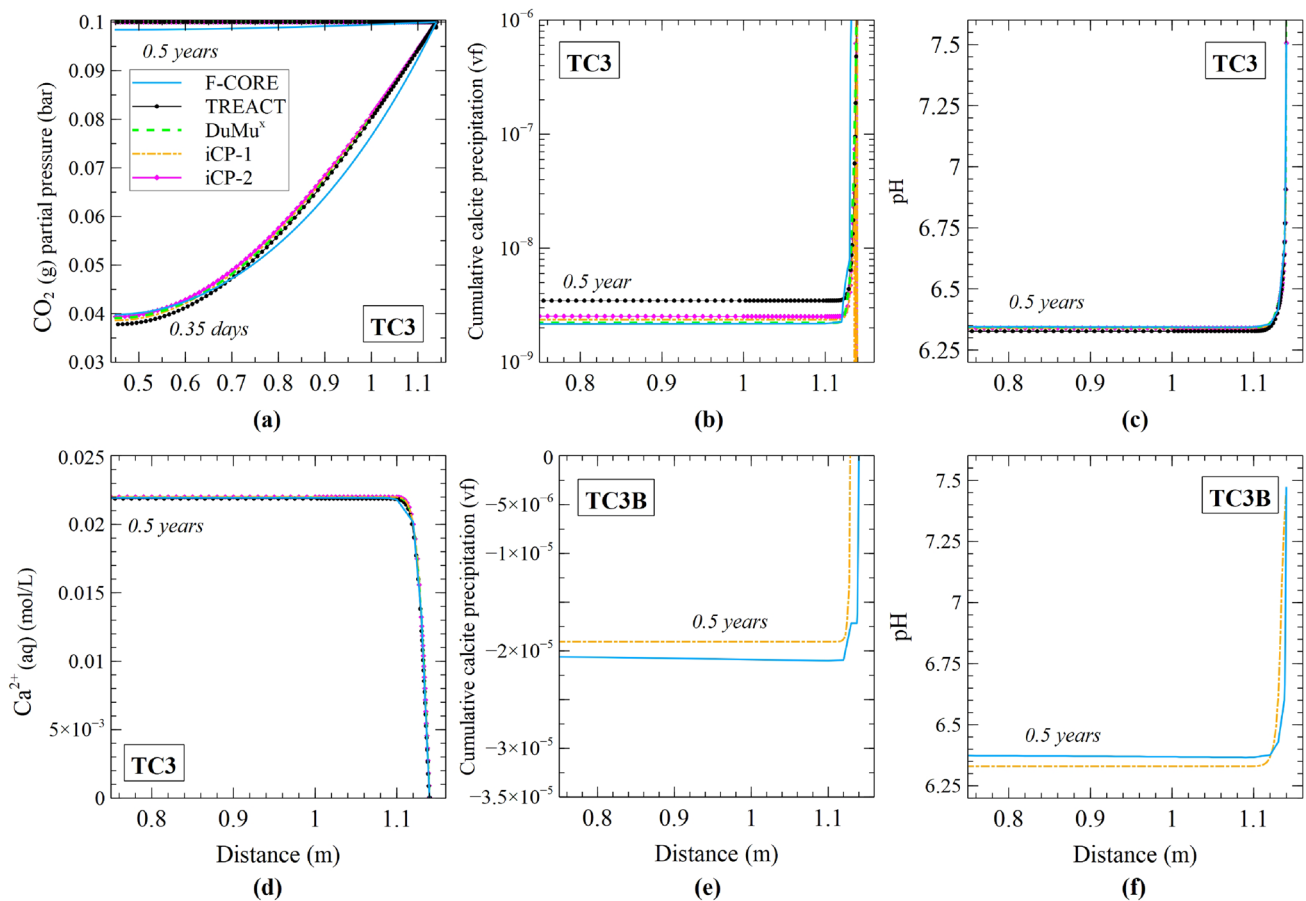


Fig. 5 Benchmarking of the spatial distribution of computed: **a** Partial pressure of $\text{CO}_{2(g)}$ for TC3 at $t = 0.35$ years and $t = 0.5$ years; **b** Cumulative calcite volume fraction (positive for precipitation) for

TC3 at $t = 0.5$ years; **c** pH for TC3 at $t = 0.5$ years; **d** Dissolved calcium for TC3 at 0.5 years; **e** Cumulative calcite volume fraction (positive for precipitation) for TC3B at $t = 0.5$ years; and **f** pH for TC3B at $t = 0.5$ years

show a fluctuation in the partial pressure between 10^{-4} and 10^{-3} years which slows down the diffusion of $\text{CO}_{2(g)}$ (see Fig. 4b). This fluctuation can be seen better when pressures are plotted versus log-time (see Fig. S4 in Supplementary Material). The computed pH increases after 0.01 years (Fig. 4d) due to the pH front associated with calcite precipitation near the right boundary (see Fig. S4 in Supplementary Material).

Case TC5. Hydration, $\text{CO}_{2(g)}$ diffusion and calcite and gypsum at equilibrium

Case TC5 is an extension of case TC4 which includes calcite and gypsum dissolution/precipitation. Similar to previous cases, the computed water content increases with time due to the water inflow. The computed $\text{CO}_{2(g)}$ partial pressure in the bentonite increases with time. Aqueous $\text{CO}_{2(aq)}$ is in equilibrium with gaseous $\text{CO}_{2(g)}$ and therefore, the increase in $\text{CO}_{2(g)}$ pressure leads to an increase in the concentration

of dissolved $\text{CO}_{2(aq)}$ and a decrease in pH. The computed $\text{CO}_{2(g)}$ partial pressures and dissolved $\text{CO}_{2(aq)}$ diffusion into bentonite follow similar patterns to those of Case TC4 (Fig. 6a). The computed concentrations of dissolved calcium and sulphate are strongly affected by dilution of the inflow water and by calcite and gypsum precipitation/dissolution. The breakthrough curves of dissolved calcium and sulphate are not smooth and show broken lines (Fig. 7a, b). Calcite precipitates while gypsum dissolves in the bentonite near the right boundary. Mineral dissolution/precipitation reactions at the final time take place in a 10 cm thick band (Fig. 7c, d). The computed concentration of dissolved Ca^{2+} decreases near the right boundary because the concentration of the boundary water is smaller than the initial concentration and due to calcite precipitation (Fig. 7a). However, it is counteracted by the release of Ca^{2+} from gypsum dissolution. Computed dissolved sulphate decreases also near the right boundary because its concentration in the boundary water is smaller than the initial concentration (Fig. 7b). On the other

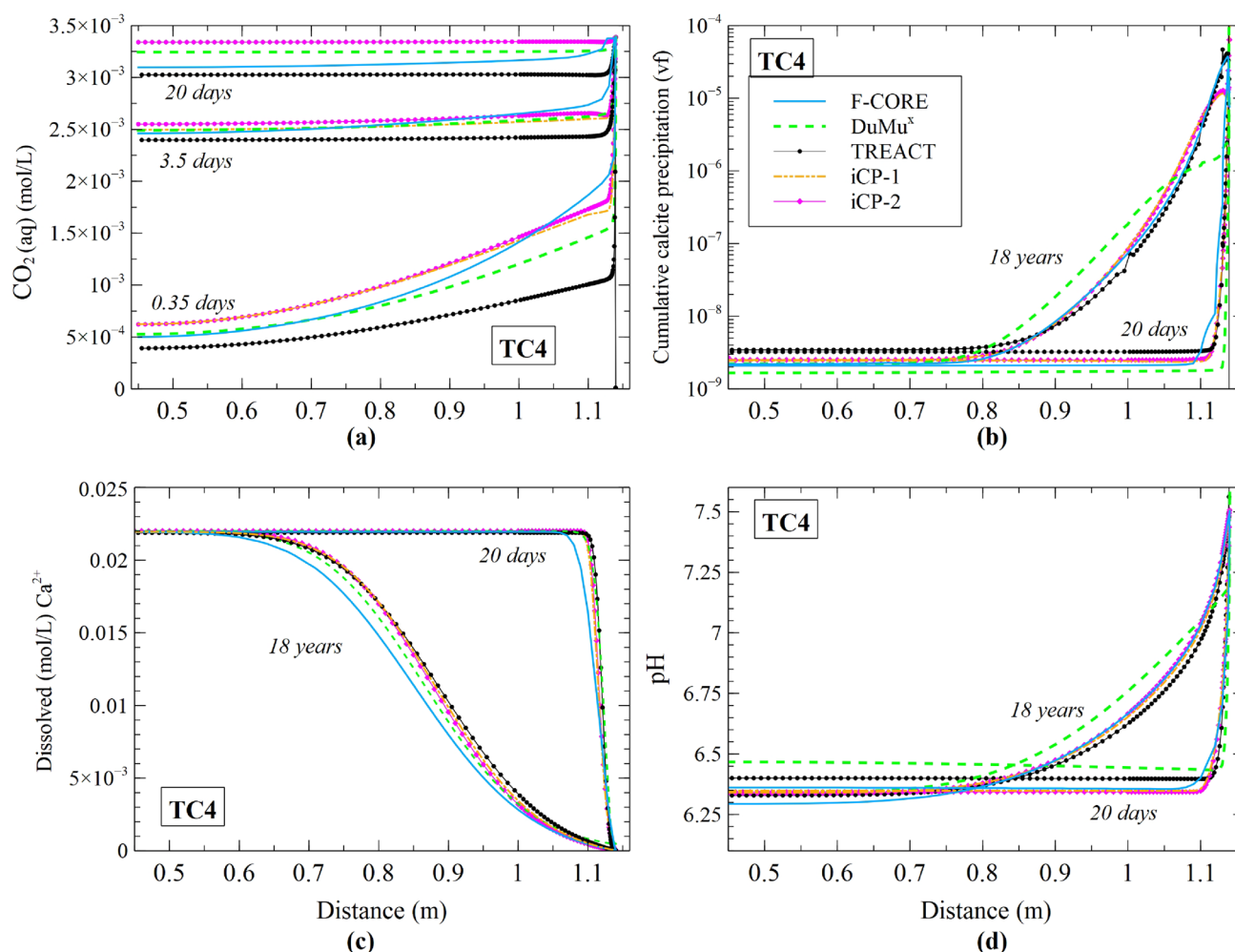


Fig. 6 Case TC4 benchmarking of the spatial distribution of computed: **a** Dissolved $\text{CO}_{2(g)}$ concentrations at $t = 0.35$ days, 3.5 days and $t = 20$ days; **b** Cumulative calcite volume fraction (positive for

precipitation) at $t = 20$ days and $t = 18$ years; **c** Dissolved calcium at $t = 20$ days and $t = 18$ years; and **d** pH at $t = 20$ days and $t = 18$ years

hand, dissolved sulphate increases near the right boundary due to gypsum dissolution. Computed pH increases near the right boundary where calcite precipitates. Case TC5 was simulated by 5 teams. The curves of computed concentration of dissolved $\text{CO}_{2(aq)}$ follow the same trends. However, there are some discrepancies which are caused by differences in the formulations implemented in different codes for gas flow at the transition from unsaturated to nearly saturated conditions similar to those mentioned in Case TC4. The concentrations of dissolved Ca^{2+} and sulphate computed with different codes are similar. However, there are small differences at the fronts similar to those reported for previous cases. The fronts of pH and total cumulative calcite precipitation and gypsum dissolution are similar for all codes.

Case TC6. Hydration, $\text{CO}_{2(g)}$ diffusion, calcite and gypsum at equilibrium and cation exchange

Case TC6 is based on Case TC5 and includes cation exchange reactions. The concentrations of dissolved species are affected by calcite and gypsum precipitation/dissolution, dilution from the hydration water and cation exchange reactions. Similar to Case TC5, the concentrations of dissolved species in TC6 decrease near the right boundary (see Fig. S5 in Material Supplementary). The computed pH increases at the locations where calcite precipitates and decreases at a point located 1.7 cm from the right boundary where calcite dissolves (Fig. 8d). Gypsum dissolution takes place during all the simulation time (Fig. 8b) while calcite shows a dissolution/precipitation front near the boundary (Fig. 8a). This front is strongly linked with dissolved Ca gets into the exchange complex at the expense of exchanged Na

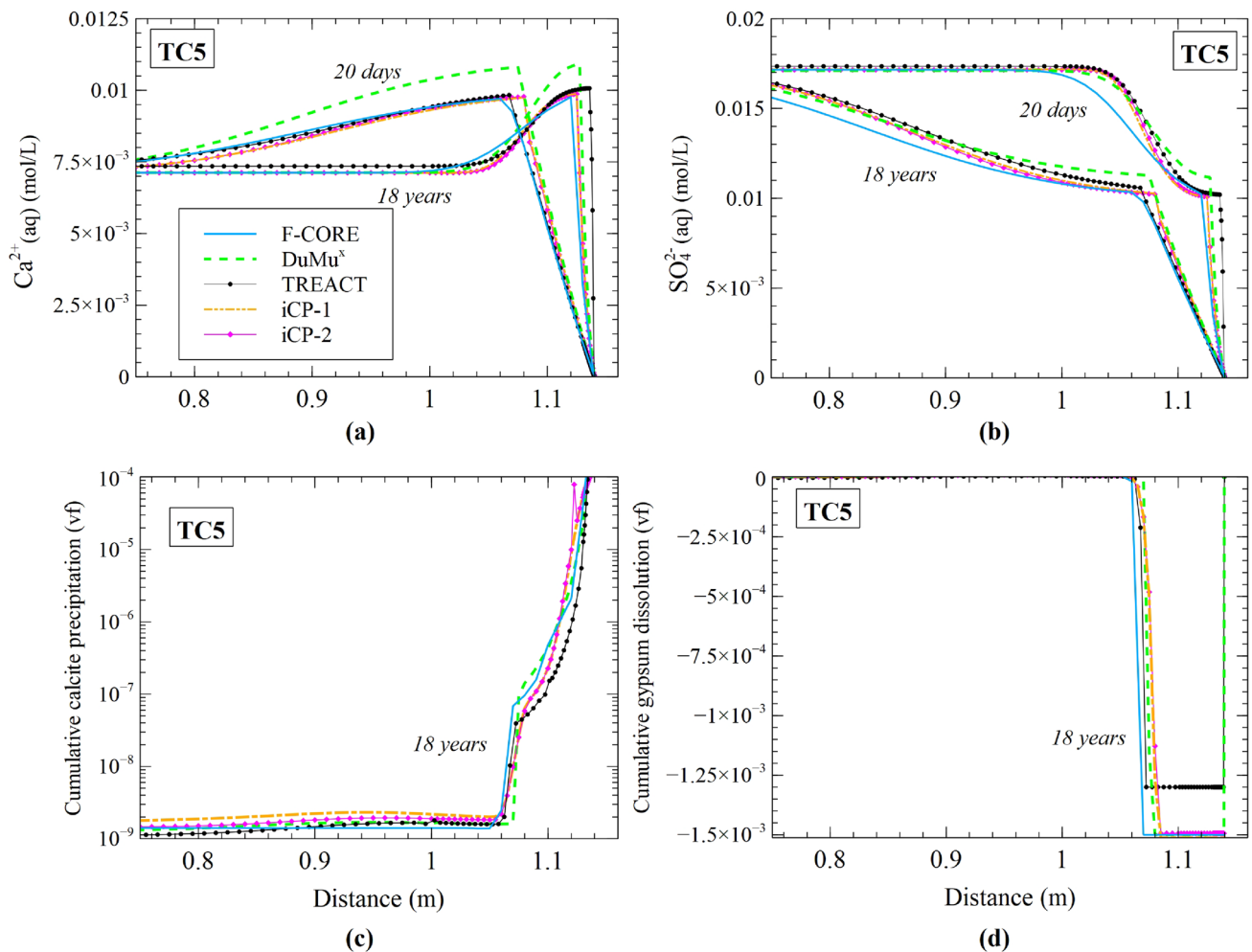


Fig. 7 TC5 benchmarking of the spatial distribution of computed: **a** Dissolved calcium at $t = 20$ days and $t = 18$ years; **b** Dissolved sulphate at $t = 20$ days and $t = 18$ years; **c** Cumulative calcite volume

fraction (positive for precipitation) at $t = 18$ years; and **d** Cumulative gypsum volume fraction (positive for precipitation) at $t = 18$ years

(X-Na). In fact, the concentration of exchanged Ca increases and that of exchanged Na decreases. The concentrations of exchanged K and Mg show small changes (Fig. 8c).

Case TC6 was simulated with 5 codes. The computed concentrations of dissolved species of different codes follow similar trends. However, there are small discrepancies in the fronts which are caused by differences in the formulations implemented in different codes for gas flow at the transition from unsaturated to nearly saturated conditions similar to those seen in previous cases. The fronts of pH and total cumulative calcite precipitation and gypsum dissolution are similar for all codes (Fig. 8).

Discussions

One of the main challenges of the benchmark had to do with ensuring that all codes and teams solved the benchmark test cases for the same flow and transport conditions, reactions

and initial and boundary conditions. To help ensuring the consistency among codes, the benchmark was designed in test cases of increasing complexity. Consistency was first warranted for conservative solute transport (Case TC1) and then for gas diffusion (TC2). Dirichlet conditions were used for gas partial pressures and concentrations of dissolved species at the inflow boundary to ensure consistency in boundary conditions. Some of the discrepancies were related to differences among codes regarding: 1) Numerical methods for spatial discretization (finite elements, finite differences and finite volumes) which may lead to oscillations and numerical dispersion, 2) Numerical schemes for coupled transport and chemistry, and 3) Formulation and parameters for activity coefficients.

The computed concentrations of dissolved species are very sensitive to water flow, solute dispersion and diffusion. Discrepancies are found in conservative tracer concentrations in Case TC1 due to differences in hydrodynamic

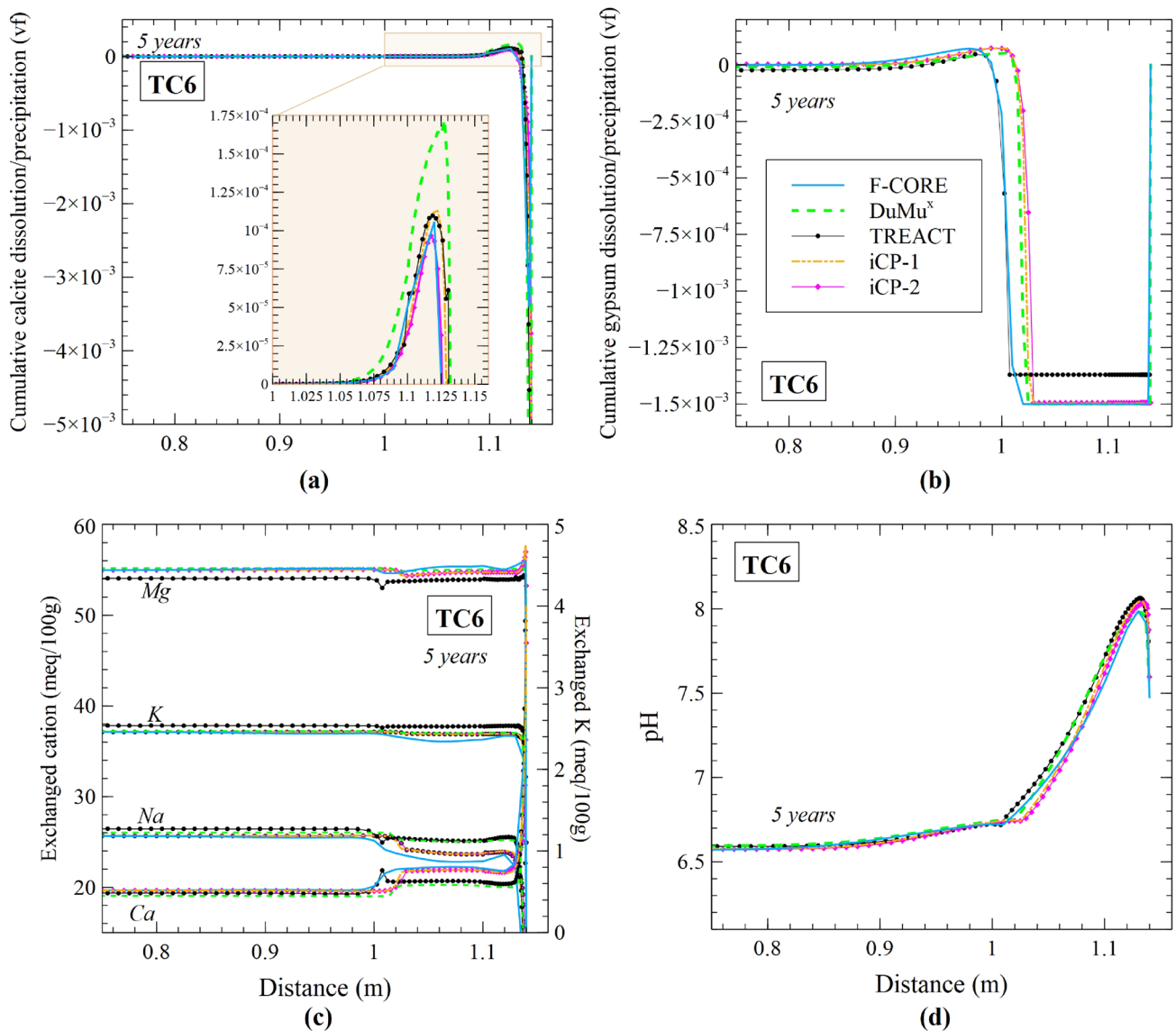


Fig. 8 Case TC6 benchmarking of the spatial distribution of computed: **a** Cumulative calcite volume fraction (positive for precipitation and negative for dissolution) at $t = 5$ years; the inner figure shows a ampliation of the cumulative calcite precipitation for $1 \text{ m} < x < 1.14$

m; **b** Cumulative gypsum volume fraction (positive for precipitation and negative for dissolution) at $t = 5$ years; **c** Concentrations of exchange cations at $t = 5$ years; and **d** pH at $t = 5$ years

dispersion because concentration profiles fully agree when water flow is disregarded. Discrepancies in the concentration of the tracer in Case TC1 are similar to those of a “dummy” tracer in test Case TC5 which is defined as the difference between the concentrations of Ca^{2+} and SO_4^{2-} (Fig. S6).

The $\text{CO}_{2(g)}$ partial pressures computed by different codes in Case TC2 follow the same trends. However, there are discrepancies in gas diffusion profiles at early times near the no-flow boundary. These discrepancies, which vanish at later times, are attributed to differences in the formulations implemented in different codes for gas flow at the transition from unsaturated to nearly saturated conditions. The

discrepancies in $\text{CO}_{2(g)}$ pressures lead to small discrepancies in computed pH.

Some codes such as iCP require the preservation of charge balance. This requirement led to the definition of Cases TC2B and TC3B, in which a more complete suite of ions and aqueous complexes were considered to ensure and preserve charge balance. Although the aqueous chemical systems of Cases TC2B and TC3B are similar to those of Cases TC2 and TC3, there are important differences in the computed pH and calcite dissolution/precipitation between Cases TC2B and TC3B and Cases TC2 and TC3. Computed pH for Cases TC2B and TC3B is smaller than those of Cases

TC2 and TC3. In addition, calcite dissolves in Cases TC2B and TC3B while it precipitates in Cases TC2 and TC3. Charge balance in Cases TC5 and TC6 was preserved by adding Na^+ and Cl^- to the chemical system.

The $\text{CO}_{2(g)}$ partial pressures computed in Case TC4 are very sensitive to mesh discretization. The gas diffusion profiles computed with different codes with a uniform mesh show significant differences. The gas diffusion coefficient decreases significantly when water flows into the column. Most codes exhibit large discretization errors for modeling gas diffusion when the mesh is not sufficiently refined. Several discretization schemes were tested. Grid refinement near the inflow boundary was performed until convergence of the numerical solution was reached. A mesh-independent solution was achieved by refining the mesh near the inflow boundary with a transition zone of gradually increasing grid size. All solutions agree when the refined grid is used. The optimum refined grid of Case TC4 was used also for the rest of the test cases. The refined grid helped to overcome the discrepancies in Cases TC5 and TC6.

All codes use the same thermodynamic data base for solving the benchmark test cases. However, there are differences among codes about the parameters and the equation used to calculate the activity coefficients of dissolved species. Activity coefficients are assumed to be constant in DuMu^X. iCP and INVERSE-FADES-CORE V2 use the extended Debye–Hückel (Eq. (18)) while TOUGHREACT uses the Helgeson–Kirkham–Flowers (HKF) extended Debye–Hückel equation (Appelo et al. 2014). The computed concentrations of dissolved species are very sensitive to the values of the activity coefficients, especially in the most reactive test cases (TC5 and TC6) in which the activity coefficients vary with time significantly. Figure S7 shows the concentrations of dissolved Ca^{2+} computed with several options for the calculation of the activity coefficients. One can see clearly that the concentrations of dissolved Ca^{2+} calculated with constant activities deviate from those calculated with time-varying activities. Tables S1 to S4, provided as in supplementary material, list the initial and final concentrations and activity coefficients calculated by different codes for Cases TC5 and TC6. Although the initial activities of the codes are similar, the final activities show significant differences because activity coefficients vary with time near the boundary (see Fig. S8).

Conclusion and perspectives

A multiphase flow and reactive transport benchmark for radioactive waste disposal has been presented. The benchmark model is based on a simplification of THCM model of the FEBEX in situ test presented by Samper et al. (2018a). The main features of the numerical model include: (1) 1D model;

(2) Unsaturated bentonite; (3) Gases (dry air and $\text{CO}_{2(g)}$); (4) Minerals (calcite and gypsum); and (5) Geochemical reactions (aqueous complexation, mineral dissolution/precipitation, cation exchange and gas dissolution/ex-solution). The following multiphase flow and reactive transport codes were used in the benchmark: INVERSE-FADES-CORE V2, DuMu^X, TOUGHREACT and iCP. A total of 6 test cases were studied with increasing complexity in flow and chemistry conditions ranging from conservative tracer migration with hydration under variably unsaturated conditions to multiphase flow with calcite and gypsum dissolution/precipitation and cation exchange reactions. All codes provide results with similar trends. Some discrepancies are found in conservative tracer concentrations due to differences in hydrodynamic dispersion. The computed $\text{CO}_{2(g)}$ partial pressures by different codes follow the same trends. However, there are some discrepancies in the gas diffusion profiles at early times near the left boundary (no flow boundary). These discrepancies which vanish at later times are caused by differences in the formulations implemented in different codes for gas flow at the transition from unsaturated to nearly saturated conditions. The discrepancies in $\text{CO}_{2(g)}$ pressures translate into small discrepancies in computed pH. The computed $\text{CO}_{2(g)}$ partial pressures are very sensitive to mesh discretization. The gas diffusion profiles computed with different codes with a uniform mesh show significant differences. All solutions tend to agree when a more refined grid is used. The concentrations of dissolved Ca computed with different codes are similar. However, there are small differences at the concentration fronts. All codes agree in the spatial distribution of pH and calcite precipitation. The diffusion of $\text{CO}_{2(g)}$ is fast. Steady and uniform pressures are reached in less than a year. Computed $\text{CO}_{2(g)}$ partial pressures show a fluctuation between 10^{-4} and 10^{-3} years which slows down the diffusion of $\text{CO}_{2(g)}$. This fluctuation is associated with chemical reactions involving CO_2 and is shown more clearly when pressures are plotted versus log-time. The computed pH increases after 0.01 years due to the pH front associated with calcite precipitation near the right boundary. There are some discrepancies in the computed concentrations of the dissolved species which are due to differences in the chemical activities of dissolved species. Some codes use different formulations of the Debye–Hückel and others assume the activities remain constant in time. Special attention was paid to ensure that all codes use the same activities. The differences in the codes caused by differences in activities have a significant impact on the fronts of dissolved Ca and sulfate.

The results of this multiphase flow code benchmark for radioactive waste disposal enhance the confidence on the use of multiphase reactive transport models. Future work should be done to extend the benchmarking to non-isothermal conditions, including vapor generation, vapor and gas transport and metallic canister corrosion.

Appendix

the initial mineral volume fractions, and the initial concentrations of exchanged ions for all test cases.

This appendix includes Tables 4, 5 and 6, which detail the initial compositions of the bentonite and granite pore water,

Table 4 Equilibrated initial pore water composition and activities, initial gas partial pressure in the bentonite and granite for TC1, TC2 and TC2B

TC1	Bentonite		Granite ($r = 1.14$ m)	
	Concentration	Activity coefficient	Concentration	Activity coefficient
Cl ⁻	1.6×10^{-1} mol/L		1.3×10^{-5} mol/L	
TC2				
H ⁺	1.799×10^{-10} mol/L	0.9921	—	—
CO _{2(aq)}	3.388×10^{-8} mol/L	1.0000	—	—
CO ₃ ²⁻	2.295×10^{-5} mol/L	—	—	—
TC2B				
H ⁺	1.847×10^{-10} mol/L	0.983	—	—
HCO ₃ ⁻	8.583×10^{-5} mol/L	0.983	—	—
Cl ⁻	10×10^{-10} mol/L	0.983	—	—
Ca ²⁺	9.656×10^{-11} mol/L	0.935	—	—
Na ⁺	1.91×10^{-4} mol/L	0.983	—	—
CO _{2(aq)}	3.43×10^{-8} mol/L	1.0	—	—
CaCl ⁺	4.63×10^{-21} mol/L	0.983	—	—
CaCO ₃	3.256×10^{-12} mol/L	1.0	—	—
Ca(OH) ⁺	8.389×10^{-14} mol/L	0.983	—	—
NaCl	5.84×10^{-15} mol/L	1.0	—	—
CaCl ₂	2.00×10^{-31} mol/L	1.0	—	—
CO ₃ ²⁻	2.325×10^{-5} mol/L	0.935	—	—
Ca(HCO ₃) ⁺	9.75×10^{-14} mol/L	0.983	—	—
Na(HCO ₃)	8.91×10^{-9} mol/L	1.0	—	—
Na(CO ₃) ⁻	7.731×10^{-5} mol/L	0.983	—	—
Na(OH)	1.839×10^{-9} mol/L	1.0	—	—
OH ⁻	5.601×10^{-5} mol/L	0.983	—	—
CO _{2(g)}	10^{-6} bar		0.1 bar	

Table 5 Equilibrated initial pore water composition and activities, initial mineral volume fractions and gas partial pressure in the bentonite and granite for TC3, TC3B and TC4

TC3 and TC4	Bentonite		Granite ($r = 1.14$ m)	
	Concentration	Activity coefficient	Concentration	Activity coefficient
H ⁺	1.77×10^{-9} mol/L	0.8122	3.201×10^{-8} mol/L	0.9819
CO _{2(aq)}	3.374×10^{-8} mol/L	1.0042	3.388×10^{-3} mol/L	1.0000
Ca ²⁺	2.195×10^{-2} mol/L	0.4405	4.799×10^{-5} mol/L	0.9295
CO ₃ ²⁻	7.701×10^{-7} mol/L	0.4447	7.707×10^{-5} mol/L	0.9296
CO _{2(g)}	10 ⁻⁶ bar		0.1 bar	
Calcite	0.01 vf		–	
TC3B				
H ⁺	1.641×10^{-9} mol/L	0.782	3.615×10^{-8} mol/L	0.938
HCO ₃ ⁻	1.41×10^{-5} mol/L	0.775	3.22×10^{-3} mol/L	0.937
Cl ⁻	4.37×10^{-2} mol/L	0.775	9.99×10^{-11} mol/L	0.937
O _{2(aq)}	1.96×10^{-31} mol/L	1.006	6.41×10^{-40} mol/L	1.000
Na ⁺	9.92×10^{-11} mol/L	0.782	3.16×10^{-3} mol/L	0.938
Ca ²⁺	2.17×10^{-2} mol/L	0.382	4.63×10^{-5} mol/L	0.775
CO ₃ ²⁻	1.03×10^{-6} mol/L	0.386	5.37×10^{-6} mol/L	0.775
CO _{2(aq)}	3.13×10^{-8} mol/L	1.006	2.29×10^{-4} mol/L	1.00
OH ⁻	1.004×10^{-5} mol/L	0.775	3.15×10^{-7} mol/L	0.937
H _{2(aq)}	1.90×10^{-31} mol/L	1.006	3.36×10^{-27} mol/L	1.00
CaCl ⁺	1.84×10^{-4} mol/L	0.782	1.84×10^{-15} mol/L	0.938
CaCO ₃	5.46×10^{-6} mol/L	1.0006	2.48×10^{-7} mol/L	1.00
Ca(OH) ⁺	1.368×10^{-6} mol/L	0.782	1.87×10^{-10} mol/L	0.938
NaCl	8.26×10^{-13} mol/L	1.006	8.76×10^{-14} mol/L	1.00
CaCl ₂	2.16×10^{-6} mol/L	1.006	7.20×10^{-26} mol/L	1.00
Ca(HCO ₃) ⁺	1.46×10^{-6} mol/L	0.782	1.45×10^{-6} mol/L	0.938
Na(HCO ₃)	4.75×10^{-16} mol/L	1.006	5.03×10^{-6} mol/L	1.00
Na(CO ₃) ⁻	7.44×10^{-16} mol/L	0.775	2.45×10^{-7} mol/L	0.937
Na(OH)	1.06×10^{-16} mol/L	1.006	1.55×10^{-10} mol/L	1.00
CO _{2(g)}	10 ⁻⁶ bar		0.1 bar	
Calcite	0.01 vf		–	

Table 6 Equilibrated initial pore water composition and activities, initial mineral volume fractions (vf) and gas partial pressure in the bentonite and granite for TC5 and TC6

TC5	Bentonite		Granite ($r = 1.14$ m)	
	Concentration	Activity coefficient	Concentration	Activity coefficient
H ⁺	1.030×10^{-9} mol/L	0.8111	3.331×10^{-8} mol/L	0.9745
CO _{2(aq)}	3.369×10^{-8} mol/L	1.0055	3.392×10^{-3} mol/L	1.0000
Ca ²⁺	7.124×10^{-3} mol/L	0.4590	4.799×10^{-5} mol/L	0.9028
SO ₄ ²⁻	1.715×10^{-2} mol/L	0.4386	7.900×10^{-5} mol/L	0.9021
Na ⁺	2.01×10^{-2} mol/L	0.8311	2.19×10^{-4} mol/L	0.9745
CO ₃ ²⁻	2.309×10^{-6} mol/L	0.4386	7.465×10^{-5} mol/L	0.9021
CO _{2(g)}	10 ⁻⁶ bar		0.1 bar	
Calcite	0.01 vf		–	
TC6				
H ⁺	1.183×10^{-9} mol/L	0.7065	3.443×10^{-8} mol/L	0.9707
CO _{2(aq)}	3.288×10^{-8} mol/L	1.0306	3.392×10^{-3} mol/L	1.0001
Ca ²⁺	1.163×10^{-2} mol/L	0.2831	4.879×10^{-5} mol/L	0.8892
Mg ²⁺	3.124×10^{-2} mol/L	0.2831	1.300×10^{-6} mol/L	0.8892
Na ⁺	1.578×10^{-1} mol/L	0.7065	3.800×10^{-4} mol/L	0.9707
K ⁺	2.086×10^{-3} mol/L	0.7065	7.800×10^{-6} mol/L	0.9707
SO ₄ ²⁻	3.039×10^{-2} mol/L	0.249	7.900×10^{-5} mol/L	0.8884
Cl ⁻	1.848×10^{-1} mol/L	0.6918	1.784×10^{-4} mol/L	0.9706
CO ₃ ²⁻	4.038×10^{-6} mol/L	0.249	7.151×10^{-5} mol/L	0.8884
CO _{2(g)}	10 ⁻⁶ bar		0.1 bar	
Calcite	0.01 vf		–	
Gypsum	0.0015 vf		–	
Exchanged Ca ²⁺	19.65 meq/100g		–	
Exchanged Mg ²⁺	54.87 meq/100g		–	
Exchanged Na ⁺	25.77 meq/100g		–	
Exchanged K ⁺	2.46 meq/100g		–	

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Data availability The authors confirm that the data supporting the findings of this study are available within the article, its supplementary materials and additional files which are openly available in ZENODO at <https://doi.org/10.5281/zenodo.13903270>.

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